

# Outline

## References:

- Strang, *Linear Algebra and its Applications*
- Meyer, *Matrix Analysis and Applied Linear Algebra*

## Topics:

1. Vector spaces
  - (a) Common examples (Euclidean n-space, spaces of polynomials, function spaces)
  - (b) Subspaces, basis and dimension
  - (c) Inner products and norms
  - (d) Orthogonality; the Projection Theorem; projection operators
  - (e) Orthogonal complements; direct sum
2. Linear Transformations
  - (a) Kernel (null space) and range (column space)
  - (b) Matrix representation (on finite-dimensional spaces)
  - (c) Change of basis and similarity transformations
  - (d) Rank theorem (the dimension of the column space of  $A \in \mathbf{R}^{m \times n}$  equals the dimension of the column space of  $A^T$ ).
  - (e) Fundamental Theorem of linear algebra (relationships between the ranges and kernels of  $A$  and  $A^T$ ).
  - (f) Determinants
3. Eigenvalues and eigenvectors
  - (a) Characteristic polynomial
  - (b) Diagonalization
  - (c) Spectral theorem for symmetric matrices
4. Jordan Canonical Form
5. Singular Value Decomposition
6. Algorithms for solving (nonsingular) linear systems; operation counts; advantages and disadvantages
  - (a) Gaussian elimination with partial pivoting
  - (b) multiplication by the inverse matrix
  - (c) Cramer's rule
- 7.

Least-squares problems

(a)

the normal equations

(b)

solving least-squares problems using the SVD

8.

The condition number of a matrix